

Solving Quadratics by Factoring

Name: _____ Date: _____ Score: _____ / 24

Q Quick Review

To solve $ax^2 + bx + c = 0$ by factoring: **(1)** move everything to one side so the other side is 0; **(2)** factor; **(3)** use the **Zero Product Property** — if a product is 0, at least one factor is 0 — and set each factor equal to 0; **(4)** solve each factor. A quadratic can have 2, 1 (double root from a perfect square), or 0 real solutions. If you can't factor, use the quadratic formula or completing the square. Factoring is fastest when the numbers are friendly.

PRACTICE

Solve each by factoring.

- | | | | |
|------------------------|-------|--------------------------|-------|
| 1. $x^2 - 7x + 12 = 0$ | _____ | 11. $x^2 + 2x = 8$ | _____ |
| 2. $x^2 + 4x - 5 = 0$ | _____ | 12. $3x^2 - 12 = 0$ | _____ |
| 3. $x^2 - 9 = 0$ | _____ | 13. $x^2 - 10x + 25 = 0$ | _____ |
| 4. $x^2 + 6x + 9 = 0$ | _____ | 14. $x^2 + 7x = 0$ | _____ |
| 5. $x^2 - x - 12 = 0$ | _____ | 15. $2x^2 - 8 = 0$ | _____ |
| 6. $x^2 + x - 6 = 0$ | _____ | 16. $x^2 - x - 20 = 0$ | _____ |
| 7. $2x^2 + 5x + 3 = 0$ | _____ | 17. $6x^2 - x - 1 = 0$ | _____ |
| 8. $x^2 + 8x + 16 = 0$ | _____ | 18. $x(x - 3) = 10$ | _____ |
| 9. $x^2 - 4x = 0$ | _____ | 19. $4x^2 - 1 = 0$ | _____ |
| 10. $x^2 = 25$ | _____ | 20. $x^2 - 2x - 15 = 0$ | _____ |

◆ Word Problems

21. A ball is launched from the ground with height model $h(t) = -16t^2 + 32t$. Besides the launch time, when does it hit the ground again?

22. A rectangular garden has area 40 square feet, and its length is 3 feet more than its width. Find the garden's dimensions.

23. A number puzzle says two consecutive even integers have a product of 48. Find the possible integers.

24. A small business uses the model $P = x^2 - 10x$ for profit, where negative values mean a loss. Find the break-even values where profit is zero.



Answer Keys

- | | |
|---|--|
| <p>1. $x = 3, 4$</p> <p>2. $x = -5, 1$</p> <p>3. $x = \pm 3$</p> <p>4. $x = -3$</p> <p>5. $x = 4, -3$</p> <p>6. $x = -3, 2$</p> <p>7. $x = -1, -\frac{3}{2}$</p> <p>8. $x = -4$</p> <p>9. $x = 0, 4$</p> <p>10. $x = \pm 5$</p> <p>11. $x = 2, -4$</p> <p>12. $x = \pm 2$</p> | <p>13. $x = 5$</p> <p>14. $x = 0, -7$</p> <p>15. $x = \pm 2$</p> <p>16. $x = 5, -4$</p> <p>17. $x = \frac{1}{2}, -\frac{1}{3}$</p> <p>18. $x = 5, -2$</p> <p>19. $x = \pm \frac{1}{2}$</p> <p>20. $x = 5, -3$</p> <p>21. $t = 2 \text{ sec}$</p> <p>22. $w = 5, \ell = 8$</p> <p>23. 6 and 8 (or $-8, -6$)</p> <p>24. $x = 0$ or $x = 10$</p> |
|---|--|

Step-by-Step Tutor Notes

1. Take it one clear step at a time and keep the original question in mind. $(x - 3)(x - 4) = 0$. So the answer is $x = 3, 4$.
2. Focus on the main idea of the problem, then simplify carefully. $(x + 5)(x - 1) = 0$. So the answer is $x = -5, 1$.
3. Focus on the main idea of the problem, then simplify carefully. $(x - 3)(x + 3) = 0$. So the answer is $x = \pm 3$.
4. Focus on the main idea of the problem, then simplify carefully. $(x + 3)^2 = 0$, double root. So the answer is $x = -3$.
5. This is a good place to slow down, check the notation, and simplify cleanly. $(x - 4)(x + 3) = 0$. So the answer is $x = 4, -3$.
6. Start with the definition the problem is testing, then apply it directly. $(x + 3)(x - 2) = 0$. So the answer is $x = -3, 2$.
7. Focus on the main idea of the problem, then simplify carefully. $(2x + 3)(x + 1) = 0$. So the answer is $x = -1, -\frac{3}{2}$.
8. This is a good place to slow down, check the notation, and simplify cleanly. $(x + 4)^2 = 0$. So the answer is $x = -4$.
9. Take it one clear step at a time and keep the original question in mind. $x(x - 4) = 0$. So the answer is $x = 0, 4$.
10. This is a good place to slow down, check the notation, and simplify cleanly. $x^2 - 25 = (x - 5)(x + 5) = 0$. So the answer is $x = \pm 5$.
11. Move all to one side: $x^2 + 2x - 8 = 0$. Factor: $(x + 4)(x - 2) = 0$.
12. Start with the definition the problem is testing, then apply it directly. $x^2 = 4$. So the answer is $x = \pm 2$.
13. Use the clue in the question first, then let the arithmetic finish the job. Perfect square. So the answer is $x = 5$.
14. Start with the definition the problem is testing, then apply it directly. $x(x + 7) = 0$. So the answer is $x = 0, -7$.
15. Start with the definition the problem is testing, then apply it directly. $x^2 = 4$. So the answer is $x = \pm 2$.
16. Use the clue in the question first, then let the arithmetic finish the job. $(x - 5)(x + 4) = 0$. So the answer is $x = 5, -4$.
17. Use the clue in the question first, then let the arithmetic finish the job. $(2x - 1)(3x + 1) = 0$. So the answer is $x = \frac{1}{2}, -\frac{1}{3}$.
18. Read the table by matching the correct row and column first, then use the count or total that fits the question. $x^2 - 3x - 10 = 0 \Rightarrow (x - 5)(x + 2) = 0$. This gives $x = 5, -2$.
19. Start with the definition the problem is testing, then apply it directly. $(2x - 1)(2x + 1) = 0$. So the answer is $x = \pm \frac{1}{2}$.
20. Take it one clear step at a time and keep the original question in mind. $(x - 5)(x + 3) = 0$. So the answer is $x = 5, -3$.
21. $-16t^2 + 32t = 0 \Rightarrow -16t(t - 2) = 0$. So $t = 0$ (start) or $t = 2$. Lands at $t = 2$.
22. $w(w + 3) = 40 \Rightarrow w^2 + 3w - 40 = 0 \Rightarrow (w + 8)(w - 5) = 0$. Positive: $w = 5, \ell = 8$.
23. $n(n + 2) = 48 \Rightarrow n^2 + 2n - 48 = 0 \Rightarrow (n + 8)(n - 6) = 0$. Positive pair: 6 and 8.
24. Name the quantities first so the model is easy to read. $x(x - 10) = 0$. Two break-even points.



Keep Building ALEKS Skills

Recommended ALEKS books and bundle



The Most Comprehensive ALEKS Math Preparation Bundle

Prep books, workbooks, full-length tests, detailed explanations, and a formula bonus file in one complete ALEKS study path.



Scan Me
Download Instantly

STUDENT FAVORITE · ALEKS Math for Beginners



ALEKS Math for Beginners 2026

Step-by-step lessons, basic study guides, topic practice, and two full-length ALEKS Math tests for students who need a calm path from review to readiness.

Great companion to these worksheets for self-study, tutoring, and classroom review.

PDF Edition



Scan Me

Amazon



Scan Me

For more ALEKS prep, visit [EffortlessMath.com/ALEKS](https://www.EffortlessMath.com/ALEKS)