

Graphing Quadratic Functions

Name: _____ Date: _____ Score: _____ / 30

Quick Review

A **quadratic function** $y = ax^2 + bx + c$ graphs as a **parabola**. Key features: the **vertex** is the highest or lowest point; the **axis of symmetry** is the vertical line through the vertex, with equation $x = -\frac{b}{2a}$. The parabola opens **up** when $a > 0$ (vertex is the minimum) and **down** when $a < 0$ (vertex is the maximum). The **y-intercept** is c (set $x = 0$). The **x-intercepts** (zeros) come from solving $ax^2 + bx + c = 0$ — they're where the parabola crosses the x -axis. To graph: find the vertex, plot a few points on each side, connect with a smooth curve.

PRACTICE

Find key features of each quadratic.

- | | | | |
|-------------------------------|-------|---|-------|
| 1. $y = x^2$ | _____ | 11. $y = (x + 1)^2 - 4$; vertex | _____ |
| 2. $y = x^2 + 5$ | _____ | 12. $y = x^2$; is (2, 4) on graph? | _____ |
| 3. $y = (x - 3)^2$ | _____ | 13. $y = -(x - 1)^2 + 3$; vertex, direction | _____ |
| 4. $y = -x^2$ | _____ | 14. $y = x^2 - 9$; x-intercepts | _____ |
| 5. $y = x^2 - 6x$ | _____ | 15. $y = 2x^2$; wider or narrower than x^2 ? | _____ |
| 6. $y = 2x^2 - 8x + 1$ | _____ | 16. $y = \frac{1}{2}x^2$; wider or narrower? | _____ |
| 7. $y = x^2 + 2x - 3$; y-int | _____ | 17. $y = x^2 + 4x + 4$; vertex | _____ |
| 8. $y = -x^2 + 4$; opens? | _____ | 18. $y = -2x^2 + 8x$; max value | _____ |
| 9. $y = 3x^2 + 6x$; vertex | _____ | 19. $y = x^2 - 1$; zeros | _____ |
| 10. $y = x^2 - 4x + 4$ | _____ | 20. $y = (x - 5)^2 + 2$; vertex | _____ |

VISUAL PRACTICE

Use the graph, table, chart, or diagram to answer the question.

21. Use the table and graph to identify the vertex.

x	-1	0	1	2	3
y	0	-3	-4	-3	0



Answer: _____

22. Use the graph to identify the vertex.



Answer: _____



◆ Word Problems

23. A ball is tossed straight up from the ground, and its height is modeled by $h(t) = -16t^2 + 32t$. Find when it reaches its peak and how high it is.

Model: _____

Answer: _____

24. A small business models profit by $P(x) = -x^2 + 10x - 9$ thousand dollars, where x is hundreds of units sold. How many units give the maximum profit, and what is that profit?

Model: _____

Answer: _____

25. A model rocket is launched from a platform, and its height in feet is $h(t) = -16t^2 + 64t + 80$. When does it hit the ground?

Model: _____

Answer: _____

26. A parabolic bridge follows $y = -\frac{1}{100}x^2 + 50$ where x is horizontal distance. Find the maximum height and the width at ground level.

Model: _____

Answer: _____

27. A fountain spray is modeled by $y = -2(x - 3)^2 + 18$, where x is horizontal distance in feet. Find the highest point and the axis of symmetry.

Model: _____

Answer: _____

28. A ball's height is $h(t) = -5t^2 + 20t + 1$ meters. Find the time and height at the peak.

Model: _____

Answer: _____

29. A small business models weekly profit by $P(x) = -(x - 6)^2 + 49$, where x is hundreds of items sold. What sales level gives maximum profit?

Model: _____

Answer: _____

30. A parabola has vertex $(-4, -2)$ and opens upward. Which is less: the value at $x = -4$ or at $x = 0$?

Model: _____

Answer: _____



Scan Me

Answer Keys

- | | |
|---|---|
| <ol style="list-style-type: none"> 1. vertex (0, 0) 2. (0, 5) 3. (3, 0) 4. opens down, vertex (0, 0) 5. $x = 3$ 6. $x = 2$ 7. (0, -3) 8. down 9. (-1, -3) 10. (2, 0) 11. (-1, -4) 12. yes 13. (1, 3), down 14. ± 3 15. narrower | <ol style="list-style-type: none"> 16. wider 17. (-2, 0) 18. $y = 8$ 19. ± 1 20. (5, 2) 21. (1, -4) 22. (1, -4) 23. $t = 1$ sec, $h = 16$ ft 24. \$16,000 at 500 units 25. $t = 5$ sec 26. 50 ft, width ≈ 141.4 ft 27. highest point (3, 18), axis $x = 3$ 28. $t = 2$ sec, $h = 21$ m 29. 600 items 30. the value at $x = -4$ |
|---|---|

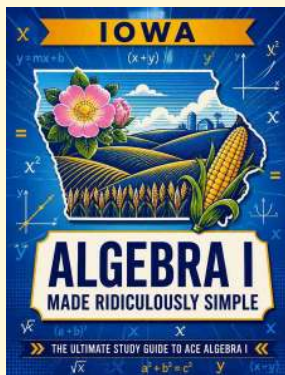
Step-by-Step Tutor Notes

1. Look for the key feature the question asks about, such as a zero, intercept, or vertex. Standard parabola: vertex at origin. That leads to vertex (0, 0).
2. Look for the key feature the question asks about, such as a zero, intercept, or vertex. Shift up 5: vertex at (0, 5). That leads to (0, 5).
3. First identify the feature of the graph or equation that matches the wording of the question. Shift right 3: vertex at (3, 0). That leads to (3, 0).
4. Use the structure of the expression to find the important point, then check that it fits the context. Negative coefficient flips it; vertex is now a max. That leads to opens down, vertex (0, 0).
5. Focus on the main idea of the problem, then simplify carefully. Axis: $-\frac{-6}{2} = 3$. So the answer is $x = 3$.
6. This is a good place to slow down, check the notation, and simplify cleanly. Axis: $-\frac{-8}{4} = 2$. So the answer is $x = 2$.
7. Take it one clear step at a time and keep the original question in mind. y -int is the constant $c = -3$. So the answer is (0, -3).
8. Focus on the main idea of the problem, then simplify carefully. $a = -1 < 0$. So the answer is down.
9. Start with the definition the problem is testing, then apply it directly. $x = -\frac{3}{6} = -1$. $y = 3(1) + 6(-1) = -3$. So the answer is (-1, -3).
10. Start with the definition the problem is testing, then apply it directly. $x = 2$, $y = 4 - 8 + 4 = 0$. (This is also $(x - 2)^2$). So the answer is (2, 0).
11. First identify the feature of the graph or equation that matches the wording of the question. Vertex form $a(x - h)^2 + k$ gives vertex $(h, k) = (-1, -4)$. That leads to (-1, -4).
12. Start with the definition the problem is testing, then apply it directly. $2^2 = 4$. \checkmark . So the answer is yes.
13. Use the structure of the expression to find the important point, then check that it fits the context. Vertex form: vertex (1, 3). $a = -1 < 0 \rightarrow$ opens down. That leads to (1, 3), down.
14. Start with the definition the problem is testing, then apply it directly. $x^2 = 9$. So the answer is ± 3 .
15. For a table question, slow down and locate the exact row, column, or cell before calculating. $|a| > 1$ stretches vertically (narrows). This gives narrower.
16. Focus on the main idea of the problem, then simplify carefully. $|a| < 1$ compresses (widens). So the answer is wider.
17. Start with the definition the problem is testing, then apply it directly. $x = -2$, $y = 4 - 8 + 4 = 0$. So the answer is (-2, 0).
18. Focus on the main idea of the problem, then simplify carefully. $x = 2$, $y = -8 + 16 = 8$. So the answer is $y = 8$.
19. Start with the definition the problem is testing, then apply it directly. $x^2 = 1$. So the answer is ± 1 .
20. Look for the key feature the question asks about, such as a zero, intercept, or vertex. Vertex form. That leads to (5, 2).
21. Look for the key feature the question asks about, such as a zero, intercept, or vertex. The smallest y -value is -4 at $x = 1$, so the vertex is (1, -4). That leads to (1, -4).
22. Use the structure of the expression to find the important point, then check that it fits the context. The lowest point of the parabola is (1, -4), so that is the vertex. That leads to (1, -4).
23. Axis: $t = -\frac{32}{-32} = 1$. $h(1) = -16 + 32 = 16$ ft. Peak at 1 sec, height 16 ft.
24. Vertex $x = -\frac{10}{2} = 5$. $P(5) = -25 + 50 - 9 = 16$ (thousand). Max profit \$16K at 500 units.
25. $h = 0$: $-16t^2 + 64t + 80 = 0$, divide by -16: $t^2 - 4t - 5 = 0 \Rightarrow (t - 5)(t + 1) = 0$. Positive answer: $t = 5$.
26. Vertex at $x = 0$: $y = 50$ (max height). Zeros: $x^2 = 5000 \Rightarrow x = \pm\sqrt{5000} \approx 70.7$. That means the bridge touches the ground about 70.7 ft left and right of center, so the total ground-level width is about 141.4 ft.
27. The equation is already in vertex form. The vertex is (3, 18), so the maximum height is 18 ft and the axis of symmetry is $x = 3$.
28. The vertex time is $t = -\frac{20}{2(-5)} = 2$. Then $h(2) = -5(4) + 40 + 1 = 21$, so the peak is 21 m at 2 sec.
29. The vertex is (6, 49). Since x is measured in hundreds of items, $x = 6$ means 600 items.
30. An upward-opening parabola has a minimum at its vertex. Since the vertex is at $x = -4$, that value is less than values away from the vertex, such as the value at $x = 0$.



Scan Me

Want a Full Algebra 1 Textbook? Try Our Iowa ISASP Made Simple Book!



Iowa ISASP Algebra I Made Ridiculously Simple

The friendly, step-by-step Algebra 1 textbook
Plain-English explanations, guided practice, and
review support.



Scan Me

Full Lessons Inside

Concepts
Practice
Mastery

Important: All our test books contain **unique, completely different tests** from each other! Each book offers fresh practice questions—no repeats!

5 Practice Tests

- ✓ 5 complete practice tests with detailed explanations
- ✓ Perfect foundation for ISASP test preparation
- ✓ Builds confidence and test-taking skills
- ✓ High-quality questions aligned with state standards

Start your practice journey!

6 Practice Tests

- ✓ 6 complete practice tests with detailed explanations
- ✓ **Unique tests**—different from the 5 tests book
- ✓ Perfect for more practice after mastering 5 tests
- ✓ Builds even more confidence and test-taking skills
- ✓ Same high-quality questions aligned with standards

Take your practice to the next level!

7 Practice Tests

- ✓ 7 complete practice tests for maximum preparation
- ✓ **Unique tests**—different from 5 and 6 tests books
- ✓ The most comprehensive practice for Algebra 1
- ✓ Ideal for students aiming for top scores
- ✓ Extensive practice builds mastery and confidence

Go all the way with comprehensive practice!

☐ STUDENT FAVORITE • Master Algebra I From the Ground Up ☐



- ✓ 100% Guaranteed
- ✓ Lifetime Support
- ✓ Trusted by Teachers

Start Your Algebra
Journey Today! →

Algebra I for Beginners

Written by a top math teacher & aligned with national and state Algebra I courses. From linear equations to graphing quadratics — explained the easy way.

- ✓ **Complete coverage** of every Algebra I concept — perfect companion to these worksheets
- ✓ **Step-by-step explanations** with worked examples on every topic
- ✓ **QR codes in every chapter** for free video lessons & bonus practice
- ✓ **2 full-length practice tests** with detailed answer keys

★ STUDENT'S #1 CHOICE ★

Teacher-recommended • 12,000+ Happy Students

↓ PDF EDITION



Scan Me

Instant download • any device

☐ PAPERBACK



Scan Me

Paperback on Amazon

Hold it in your hands

Pair these free worksheets with *Algebra I for Beginners* and you have a complete self-paced course — concept lessons, daily practice, and full exam-style reviews, all in one path. →

EffortlessMath.com/product/algebra-i-for-beginners