

Graphing Proportional Relationships

Name: _____

Date: _____

Score: _____ / 24

Q Quick Review

A **proportional relationship** connects two quantities so that their ratio is always the same. You can write it as $y = kx$, where k is the **constant of proportionality** — the number you multiply x by to get y . To find k from a point (x, y) , just divide: $k = \frac{y}{x}$. When you graph $y = kx$, you always get a *straight line through the origin* $(0, 0)$, and k is the **slope** of that line — the steepness. The bigger k is, the steeper the line climbs.

◊ **Example:** A car travels 150 miles in 3 hours at a steady speed. Find the constant of proportionality and write the equation.
 ⇒ The two quantities here are distance y and time x , and a steady speed means they are proportional. To find k , divide distance by time: $k = \frac{150}{3} = 50$. That 50 is the speed in miles per hour — it tells us how many miles the car covers each hour. Now we just slot k into $y = kx$ to get $y = 50x$. The graph would be a straight line through the origin rising 50 for every 1 hour.

Answer: $k = 50$, $y = 50x$

PRACTICE

Find the constant of proportionality k , or use $y = kx$ as needed.

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| 1. $y = kx$ through $(1, 4)$; $k = ?$ | _____ | 11. $k = 11$, $x = 4$; $y = ?$ | _____ |
| 2. $y = kx$ through $(1, 9)$; $k = ?$ | _____ | 12. $k = \frac{2}{3}$, $x = 9$; $y = ?$ | _____ |
| 3. $y = kx$ through $(2, 10)$; $k = ?$ | _____ | 13. $k = 5$, $y = 35$; $x = ?$ | _____ |
| 4. $y = kx$ through $(3, 21)$; $k = ?$ | _____ | 14. $k = 9$, $y = 63$; $x = ?$ | _____ |
| 5. $y = kx$ through $(4, 12)$; $k = ?$ | _____ | 15. $k = 4$, $y = 30$; $x = ?$ | _____ |
| 6. $y = kx$ through $(5, 40)$; $k = ?$ | _____ | 16. Is $y = 3x$ proportional? | _____ |
| 7. $y = kx$ through $(6, 9)$; $k = ?$ | _____ | 17. Is $y = 2x + 5$ proportional? | _____ |
| 8. $y = kx$ through $(8, 2)$; $k = ?$ | _____ | 18. $y = kx$ through $(10, 4)$; $k = ?$ | _____ |
| 9. $k = 6$, $x = 7$; $y = ?$ | _____ | 19. Slope of $y = 7x$ | _____ |
| 10. $k = 2.5$, $x = 8$; $y = ?$ | _____ | 20. Unit rate: \$18 for 3 lb | _____ |

◆ Word Problems

21. A printer prints 36 pages in 4 minutes at a steady rate. Write an equation relating pages y to minutes x , and find how many pages it prints in 9 minutes. _____
22. At a market, 5 apples cost \$2. The cost is proportional to the number of apples. How much do 20 apples cost? _____
23. A cyclist rides at a constant speed and covers 24 km in 2 hours. Two graphs are compared: cyclist A has $y = 12x$ and cyclist B covers 24 km in 2 hours. Who is faster, or are they the same? _____
24. A faucet fills a tub proportionally, putting in 7 gallons every 2 minutes. How long does it take to fill a 35-gallon tub? _____



Answer Keys

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| <p>1. $k = 4$</p> <p>2. $k = 9$</p> <p>3. $k = 5$</p> <p>4. $k = 7$</p> <p>5. $k = 3$</p> <p>6. $k = 8$</p> <p>7. $k = \frac{3}{2}$</p> <p>8. $k = \frac{1}{4}$</p> <p>9. $y = 42$</p> <p>10. $y = 20$</p> <p>11. $y = 44$</p> <p>12. $y = 6$</p> | <p>13. $x = 7$</p> <p>14. $x = 7$</p> <p>15. $x = \frac{15}{2}$</p> <p>16. yes</p> <p>17. no</p> <p>18. $k = \frac{2}{5}$</p> <p>19. 7</p> <p>20. \$6 per lb</p> <p>21. $y = 9x$; 81 pages</p> <p>22. \$8</p> <p>23. the same speed</p> <p>24. 10 minutes</p> |
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Step-by-Step Explanations

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| <p>1. With $x = 1$, the value of y is the constant: $k = \frac{4}{1} = 4$.</p> <p>2. At $x = 1$, $k = \frac{9}{1} = 9$. The point $(1, k)$ always reveals k.</p> <p>3. Divide y by x: $k = \frac{10}{2} = 5$.</p> <p>4. $k = \frac{21}{3} = 7$, the same ratio every time.</p> <p>5. $k = \frac{12}{4} = 3$ — y is always three times x.</p> <p>6. $k = \frac{40}{5} = 8$.</p> <p>7. $k = \frac{9}{6} = \frac{3}{2}$ — k can be a fraction.</p> <p>8. $k = \frac{2}{8} = \frac{1}{4}$, a value less than 1.</p> <p>9. Use $y = kx$: $y = 6 \times 7 = 42$.</p> <p>10. $y = 2.5 \times 8 = 20$.</p> <p>11. $y = 11 \times 4 = 44$.</p> <p>12. $y = \frac{2}{3} \times 9 = 6$.</p> <p>13. From $y = kx$, divide: $x = \frac{35}{5} = 7$.</p> | <p>14. $x = \frac{63}{9} = 7$.</p> <p>15. $x = \frac{30}{4} = \frac{15}{2}$.</p> <p>16. It has the form $y = kx$ with $k = 3$ and passes through $(0, 0)$, so yes.</p> <p>17. The $+5$ shifts the line off the origin, so it is <i>not</i> proportional.</p> <p>18. $k = \frac{4}{10} = \frac{2}{5}$.</p> <p>19. In $y = kx$, the constant k is the slope, so the slope is 7.</p> <p>20. Divide cost by weight: $\frac{18}{3} = 6$ dollars per pound.</p> <p>21. The rate is $k = \frac{36}{4} = 9$ pages per minute, so $y = 9x$. In 9 minutes: $y = 9 \times 9 = 81$ pages.</p> <p>22. The unit cost is $k = \frac{2}{5} = 0.40$ dollars per apple. For 20 apples: $0.40 \times 20 = \\$8$.</p> <p>23. Cyclist B's rate is $\frac{24}{2} = 12$ km/h, the same k as cyclist A's $y = 12x$. Equal constants mean equal speeds.</p> <p>24. The rate is $\frac{7}{2} = 3.5$ gallons per minute. Time = $\frac{35}{3.5} = 10$ minutes.</p> |
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