

Estimating Irrational Numbers

Name: _____ Date: _____ Score: _____ / 24

Q Quick Review

You can pin down an irrational square root *without* a calculator by trapping it between two whole numbers. To estimate \sqrt{n} , find the **perfect square just below** n and the **perfect square just above** it. The square root of n lands between their roots. For a closer guess, check which perfect square n is *nearer* to — that tells you which whole number \sqrt{n} is closer to. You can even test a decimal: square it and see if the result is just under or just over n . This same idea lets you place $\pi \approx 3.14$ on a number line too.

◇ **Example:** Between which two consecutive whole numbers does $\sqrt{52}$ lie?
 ⇒ List the perfect squares around 52: we have $49 = 7^2$ and $64 = 8^2$, and 52 sits between them. Taking square roots keeps the order, so $7 < \sqrt{52} < 8$. Want to go further? Since 52 is only 3 away from 49 but 12 away from 64, $\sqrt{52}$ is *much closer* to 7 — a good estimate is about 7.2.

Answer: $7 < \sqrt{52} < 8$

PRACTICE

Estimate each value or place it between two consecutive whole numbers.

- | | | | |
|----------------|-------|--|-------|
| 1. $\sqrt{10}$ | _____ | 11. $\sqrt{17}$ (nearest whole number) | _____ |
| 2. $\sqrt{5}$ | _____ | 12. $\sqrt{83}$ (nearest whole number) | _____ |
| 3. $\sqrt{30}$ | _____ | 13. $\sqrt{38}$ (nearest whole number) | _____ |
| 4. $\sqrt{2}$ | _____ | 14. $\sqrt{24}$ (nearest whole number) | _____ |
| 5. $\sqrt{40}$ | _____ | 15. $\sqrt{90}$ (nearest whole number) | _____ |
| 6. $\sqrt{70}$ | _____ | 16. $\sqrt{12}$ (nearest tenth) | _____ |
| 7. $\sqrt{99}$ | _____ | 17. $\sqrt{20}$ (nearest tenth) | _____ |
| 8. $\sqrt{3}$ | _____ | 18. $\sqrt{7}$ (nearest tenth) | _____ |
| 9. $\sqrt{55}$ | _____ | 19. π (between two whole numbers) | _____ |
| 10. $\sqrt{8}$ | _____ | 20. 2π (nearest whole number) | _____ |

◆ Word Problems

- A square rug has an area of 45 square feet. Between which two whole numbers is the length of one side? _____
- A ladder leans so its base is $\sqrt{60}$ feet from a wall. Estimate this distance to the nearest whole number of feet. _____
- A circular pond has a radius of 5 m, so its circumference is 10π m. Estimate the circumference to the nearest whole meter. _____
- On a number line, would $\sqrt{50}$ sit to the left or right of 7? Explain. _____



Answer Keys

- | | |
|---|--|
| <p>1. $3 < \sqrt{10} < 4$</p> <p>2. $2 < \sqrt{5} < 3$</p> <p>3. $5 < \sqrt{30} < 6$</p> <p>4. $1 < \sqrt{2} < 2$</p> <p>5. $6 < \sqrt{40} < 7$</p> <p>6. $8 < \sqrt{70} < 9$</p> <p>7. $9 < \sqrt{99} < 10$</p> <p>8. $1 < \sqrt{3} < 2$</p> <p>9. $7 < \sqrt{55} < 8$</p> <p>10. $2 < \sqrt{8} < 3$</p> <p>11. 4</p> <p>12. 9</p> | <p>13. 6</p> <p>14. 5</p> <p>15. 9</p> <p>16. 3.5</p> <p>17. 4.5</p> <p>18. 2.6</p> <p>19. $3 < \pi < 4$</p> <p>20. 6</p> <p>21. between 6 and 7 feet</p> <p>22. about 8 feet</p> <p>23. about 31 meters</p> <p>24. to the right of 7</p> |
|---|--|

Step-by-Step Explanations

- | | |
|--|--|
| <p>1. 10 is between $9 = 3^2$ and $16 = 4^2$, so $\sqrt{10}$ is between 3 and 4.</p> <p>2. 5 sits between $4 = 2^2$ and $9 = 3^2$, so $2 < \sqrt{5} < 3$.</p> <p>3. 30 is between $25 = 5^2$ and $36 = 6^2$, giving $5 < \sqrt{30} < 6$.</p> <p>4. 2 is between $1 = 1^2$ and $4 = 2^2$, so $\sqrt{2}$ is between 1 and 2.</p> <p>5. 40 falls between $36 = 6^2$ and $49 = 7^2$, so $6 < \sqrt{40} < 7$.</p> <p>6. 70 is between $64 = 8^2$ and $81 = 9^2$, giving $8 < \sqrt{70} < 9$.</p> <p>7. 99 sits between $81 = 9^2$ and $100 = 10^2$, so $9 < \sqrt{99} < 10$.</p> <p>8. 3 is between 1 and 4, so $\sqrt{3}$ is between 1 and 2.</p> <p>9. 55 is between $49 = 7^2$ and $64 = 8^2$, so $7 < \sqrt{55} < 8$.</p> <p>10. 8 is between 4 and 9, so $\sqrt{8}$ lies between 2 and 3.</p> <p>11. 17 is between $16 = 4^2$ and $25 = 5^2$ but only 1 away from 16, so $\sqrt{17} \approx 4$.</p> <p>12. 83 is between 81 and 100; it is much closer to $81 = 9^2$, so $\sqrt{83} \approx 9$.</p> <p>13. 38 is between $36 = 6^2$ and 49, and only 2 away from 36, so $\sqrt{38} \approx 6$.</p> <p>14. 24 is between 16 and 25; it is just 1 away from $25 = 5^2$, so $\sqrt{24} \approx 5$.</p> | <p>15. 90 is between $81 = 9^2$ and 100, and closer to 81, so $\sqrt{90} \approx 9$.</p> <p>16. $3.4^2 = 11.56$ and $3.5^2 = 12.25$; since 12 is closer to 12.25, $\sqrt{12} \approx 3.5$.</p> <p>17. $4.4^2 = 19.36$ and $4.5^2 = 20.25$; 20 is closer to 20.25, so $\sqrt{20} \approx 4.5$.</p> <p>18. $2.6^2 = 6.76$ and $2.7^2 = 7.29$; 7 is closer to 6.76, so $\sqrt{7} \approx 2.6$.</p> <p>19. $\pi = 3.14159\dots$, which sits between the whole numbers 3 and 4.</p> <p>20. $2\pi \approx 2 \times 3.14 = 6.28$, which rounds to 6.</p> <p>21. The side is $\sqrt{45}$. Since 45 is between $36 = 6^2$ and $49 = 7^2$, the side length is between 6 and 7 feet.</p> <p>22. 60 is between $49 = 7^2$ and $64 = 8^2$, and it is much closer to 64, so $\sqrt{60} \approx 8$ feet.</p> <p>23. Using $\pi \approx 3.14$, the circumference $10\pi \approx 10 \times 3.14 = 31.4$ m, which rounds to 31 m.</p> <p>24. $7 = \sqrt{49}$, and $50 > 49$, so $\sqrt{50} > 7$. That places $\sqrt{50}$ just to the right of 7 on the number line.</p> |
|--|--|



Want Even More Practice? Check Out Our Other West Virginia WVGSA Test Books!



West Virginia WVGSA Grade 8 Math Preparation Bundle

18 full-length practice tests across three books
(5 + 6 + 7)

No repeated questions—maximum practice value!



18 Tests!
3 Books
One Bundle

Important: All our test books contain **unique, completely different tests** from each other! Each book offers fresh practice questions—no repeats!

5 Practice Tests

- ✓ 5 complete practice tests with detailed explanations
- ✓ Perfect foundation for WVGSA test preparation
- ✓ Builds confidence and test-taking skills
- ✓ High-quality questions aligned with state standards

Start your practice journey!

6 Practice Tests

- ✓ 6 complete practice tests with detailed explanations
- ✓ **Unique tests**—different from the 5 tests book
- ✓ Perfect for more practice after mastering 5 tests
- ✓ Builds even more confidence and test-taking skills
- ✓ Same high-quality questions aligned with standards

Take your practice to the next level!

7 Practice Tests

- ✓ 7 complete practice tests for maximum preparation
- ✓ **Unique tests**—different from 5 and 6 tests books
- ✓ The most comprehensive practice for Grade 8
- ✓ Ideal for students aiming for top scores
- ✓ Extensive practice builds mastery and confidence

Go all the way with comprehensive practice!