

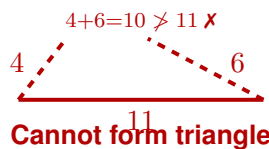
Triangle Inequality Theorem

Name: _____

Date: _____

Score: _____ / 17

Can any three lengths make a triangle? Not always—and the **Triangle Inequality Theorem** tells you exactly when it works! The rule: the sum of any two sides must be *greater than* the third side, so you check $a + b > c$, $a + c > b$, and $b + c > a$. A quick shortcut: just add the two *shortest* sides—if that total beats the longest side, you are good. The theorem also lets you find the range for a missing side: it must be greater than the difference of the other two and less than their sum. Handy for construction, design, and any problem where you need to know if a triangle is even possible!



Key Concepts & Quick Review

Triangle Inequality Theorem: For any triangle with sides a , b , and c :

$$a + b > c, \quad a + c > b, \quad b + c > a$$

All three conditions must be true.

Quick check: Add the two *shortest* sides. If their sum is greater than the longest side, a triangle can be formed.

Finding a range for the third side: Given two sides of lengths a and b (with $a \geq b$), the third side c must satisfy

$$a - b < c < a + b$$

Examples

① Can a triangle have side lengths 4, 6, and 11?

Think It Through: Here is the key test: add the two *shortest* sides and see whether that total is greater than the longest side. The two shortest are 4 and 6, and $4 + 6 = 10$. Is $10 > 11$? Nope—10 falls short! Because the two shorter sticks are not long enough to "reach around" the longest one, these three lengths **cannot** form a triangle.

Answer: No

② Two sides of a triangle are 5 and 9. Find the range of possible lengths for the third side.

Think It Through: Think of it this way: the third side has to be short enough that it does not "stretch past" the other two, but long enough that it can actually close the triangle. Subtract the shorter from the longer to get the minimum: $9 - 5 = 4$. Add them for the maximum: $9 + 5 = 14$. So the third side c must



satisfy $4 < c < 14$. (Notice: 4 and 14 themselves are *not* included—those would make a flat line, not a triangle!)

 **Answer:** $4 < c < 14$

Practice Problems

Determine whether the three lengths can form a triangle. Write **Yes** or **No**. For range problems, give the range.

- Can side lengths 3, 5, and 7 form a triangle? Write Yes or No. _____
- Can side lengths 1, 2, and 5 form a triangle? Write Yes or No. _____
- Can side lengths 6, 8, and 10 form a triangle? Write Yes or No. _____
- Can side lengths 4, 4, and 9 form a triangle? Write Yes or No. _____
- Can side lengths 5, 5, and 5 form a triangle? Write Yes or No. _____
- Can side lengths 2, 3, and 6 form a triangle? Write Yes or No. _____
- Can side lengths 7, 10, and 12 form a triangle? Write Yes or No. _____
- Can side lengths 1, 1, and 2 form a triangle? Write Yes or No. _____
- Can side lengths 9, 12, and 15 form a triangle? Write Yes or No. _____
- Can side lengths 3, 4, and 8 form a triangle? Write Yes or No. _____
- Two sides of a triangle are 5 and 8. Find the possible range for the third side c . _____
- Two sides of a triangle are 3 and 10. Find the possible range for the third side c . _____
- Two sides of a triangle are 6 and 6. Find the possible range for the third side c . _____
- Two sides of a triangle are 2 and 7. Find the possible range for the third side c . _____
- Two sides of a triangle are 4 and 11. Find the possible range for the third side c . _____

Study Tips

-  The fastest check: **add the two smallest**. If that sum beats the largest side, a triangle is possible.
-  If $a + b = c$ (exactly equal), the three segments form a straight line, **not** a triangle.
-  For the range of a missing side, remember the formula $|a - b| < c < a + b$ and note the **strict** inequality (no \leq).

Word Problems

- You have three sticks measuring 8 cm, 15 cm, and 6 cm. Can you use them to build a triangular frame? _____
- Two sides of a garden bed are 12 feet and 7 feet long. A landscaper is cutting a third piece of edging. What are the shortest and longest whole-number lengths that will form a triangular bed? _____



Answer Keys

- | | |
|---|--|
| <p>1) yes
2) no
3) yes
4) no
5) yes
6) no
7) yes
8) no
9) yes</p> | <p>10) no
11) $3 < c < 13$
12) $7 < c < 13$
13) $0 < c < 12$
14) $5 < c < 9$
15) $7 < c < 15$
16) No; triangle inequality fails
17) The third side can be 6, 7, 8, ..., 18 ft (whole numbers from 6 to 18 inclusive).</p> |
|---|--|

Step-by-Step Explanations

Strategy: For Factoring Expressions, look for a common factor and rewrite the expression as a product that could multiply back. For factoring, look for the common factor before trying anything more complicated.

Practice 1: $4x+8$ **Answer:** $4(x+2)$

For the first worked item, isolate the target variable by undoing the operation attached to it.

Practice 15: $7p^2 - 14p$ **Answer:** $7p(p-2)$

Near the end of this topic, collect like terms before solving so the inequality has one variable term.

Word-problem notes:

16. Answer: $12(2n+3)$; at $n=5$: $12(13) = 156$ tiles; dimensions 12×13 .

Factor the expression by pulling out the greatest common factor of $24n$ and 36 , which is 12 . That gives $24n + 36 = 12(2n + 3)$. This shows one possible patio layout is 12 rows by $(2n + 3)$ columns. When $n = 5$, the second factor is $2(5) + 3 = 13$, so the patio needs $12 \times 13 = 156$ tiles. The factored form turns the total tile count into a dimensions picture.

17. Answer: $5(p+3)$; reveals a \$5 unit price; $p=8$: $5(8) + 15 = 55$ and $5(11) = 55$ ✓.

The greatest common factor in $5p + 15$ is 5 , so the factored form is $5(p + 3)$. This shows that the revenue is built from groups of \$5. When $p = 8$, the original form gives $5(8) + 15 = 40 + 15 = 55$. The factored form gives $5(8 + 3) = 5(11) = 55$. Since both methods give the same result, the factoring is correct.



Want Even More Practice?

Check Out Our Other West Virginia WVGSA Test Books!



West Virginia WVGSA Grade 7 Math Preparation Bundle

18 full-length practice tests across three books (5 + 6 + 7)

No repeated questions—maximum practice value!



18 Tests!
3 Books
One Bundle

Important: All our test books contain **unique, completely different tests** from each other! Each book offers fresh practice questions—no repeats!

5 Practice Tests

- ✓ 5 complete practice tests with detailed explanations
- ✓ Perfect foundation for WVGSA test preparation
- ✓ Builds confidence and test-taking skills
- ✓ High-quality questions aligned with state standards

Start your practice journey!

6 Practice Tests

- ✓ 6 complete practice tests with detailed explanations
- ✓ **Unique tests**—different from the 5 tests book
- ✓ Perfect for more practice after mastering 5 tests
- ✓ Builds even more confidence and test-taking skills
- ✓ Same high-quality questions aligned with standards

Take your practice to the next level!

7 Practice Tests

- ✓ 7 complete practice tests for maximum preparation
- ✓ **Unique tests**—different from 5 and 6 tests books
- ✓ The most comprehensive practice for Grade 7
- ✓ Ideal for students aiming for top scores
- ✓ Extensive practice builds mastery and confidence

Go all the way with comprehensive practice!