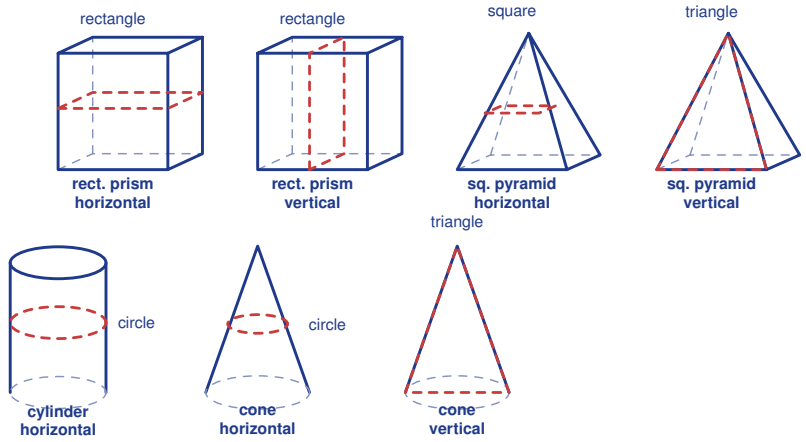
Cross Sections of 3-D Figures

Name: _____	Date: _____	Score: _____ / 17

Imagine slicing a 3-D solid with a perfectly flat plane—the shape you see on the cut surface is called a **cross section**. The fascinating part is that the *same* solid can produce different cross sections depending on how you make the cut! A horizontal slice, a vertical slice, and a diagonal slice through a cylinder, for example, give very different shapes. Cross sections are a wonderfully visual way to connect 2-D and 3-D geometry.



Key Concepts & Quick Review

- **Rectangular prism:** horizontal → rectangle; vertical (parallel to face) → rectangle; diagonal → rectangle or parallelogram.
- **Square pyramid:** horizontal → square (smaller toward apex); vertical through apex → triangle.
- **Cylinder:** horizontal → circle; vertical → rectangle; diagonal → ellipse.
- **Cone:** horizontal → circle; vertical through apex → triangle (isosceles).
- **Sphere:** any cut through centre → circle (great circle); off-centre → smaller circle.

Examples

① A rectangular prism ($10\ cm \times 6\ cm \times 4\ cm$) is sliced horizontally halfway up. Describe the cross section and find its area.

Think It Through: A horizontal cut is parallel to the base, so the cross section has the same shape as the base. The base of this prism is a $10\ cm$ by $6\ cm$ rectangle, so the slice is also a rectangle with those dimensions. Its area is therefore $10 \times 6 = 60\ cm^2$. The height of the cut does not change the shape or area in a prism like this.

Answer: *Rectangle* 10×6*; area* $= 60\ cm^2$

② A square pyramid with base $8\ cm$ is cut by a plane parallel to the base at half the vertical height. What shape is the cross section and what is its side length?

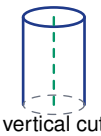
Think It Through: A cut parallel to the base of a pyramid makes a smaller, similar copy of the base, so the cross section is a square. Because the cut is halfway from the apex to the base, every linear measurement is scaled by $\frac{1}{2}$. That makes the side length $\frac{1}{2} \times 8 = 4\ cm$. Once the side is known, the area is $4^2 = 16\ cm^2$.

Answer: *Square with side* $4\ cm$*; area* $= 16\ cm^2$

Practice Problems

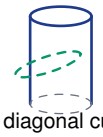
Name the shape of each cross section or find the area/dimensions asked.

1. A cube is sliced by a horizontal plane parallel to its base. What is the cross-section shape? _____
2. A cube is sliced by a vertical plane parallel to one face. What is the cross-section shape? _____
3. A cube is sliced by a diagonal plane that cuts across opposite faces. What is the cross-section shape? _____
4. A square pyramid is sliced by a horizontal plane parallel to its base. What is the cross-section shape? _____
5. A square pyramid is sliced by a vertical plane through its apex. What is the cross-section shape? _____
6. A cylinder is sliced by a horizontal plane parallel to its circular bases. What is the cross-section shape? _____
7. A cylinder is sliced by a vertical plane through its height. What is the cross-section shape? _____



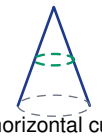
vertical cut

8. A cylinder is sliced by a diagonal plane that is not parallel to the base. What is the cross-section shape? _____



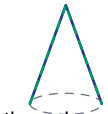
diagonal cut

9. A cone is sliced by a horizontal plane parallel to its base. What is the cross-section shape? _____



horizontal cut

10. A cone is sliced by a vertical plane through its apex. What is the cross-section shape? _____



11. A sphere is sliced by any flat plane through its center. What is the cross-section shape? _____

12. A rectangular prism measures 10 by 8 by 6. A horizontal cut is parallel to the 10 by 8 base. Find the cross-section area. _____

13. A square pyramid has base side length 12. A horizontal cut is made one-third of the way up from the base. Find the side length of the cross section. _____

14. A square pyramid has base side length 9. A horizontal cut is made two-thirds of the way up from the base. Find the side length of the cross section. _____

15. A cylinder has radius 5. A horizontal cut is parallel to its base. Find the cross-section area. _____

Study Tips

- **Direction determines shape.** A cut parallel to the base gives a scaled copy of the base. A cut through the apex gives a triangle.
- For a pyramid cut at fraction f of the height from the apex, every linear dimension of the cross section is f times the base dimension.
- Real-world cross sections appear in MRI/CT scans, sawing timber, cooking (slicing fruit), and engineering blueprints — recognising them is a genuinely useful skill!

Word Problems

16. A block of cheese is shaped like a rectangular prism, $24\ cm$ long, $12\ cm$ wide, and $8\ cm$ tall. A chef slices it with three different cuts: (a) horizontally at half-height, (b) vertically along the length, (c) diagonally from one top edge to the opposite bottom edge. Describe the shape and dimensions of each cross section, and find its area. _____

17. A traffic cone is a solid cone with base radius $15\ cm$ and height $40\ cm$. A road worker cuts it with a horizontal plane $10\ cm$ from the top. What shape is the cross section? Using similar triangles, find the radius of the cross section. Find the area of the cross section. _____

Answer Keys

1) square
2) rectangle
3) rectangle or parallelogram
4) square
5) triangle
6) circle
7) rectangle
8) ellipse
9) circle
10) triangle
11) circle
12) 80
13) 8
14) 3
15) 78.5
16) (a) $288\ cm^2$; (b) $192\ cm^2$; (c) rectangle, about $345.6\ cm^2$
17) Circle; radius $3.75\ cm$; area about $44.2\ cm^2$

Step-by-Step Explanations

Strategy: For Area of Circles, use radius for circle area every time, dividing the diameter by two first if the problem gives diameter. For circle area, mark the radius first; the formula depends on it.

Practice 1: Find the area of a circle with radius $4\ cm$. **Answer:** $50.24\ cm^2$
For the first worked item, use A equals pi r squared, making sure r is the radius.

Practice 15: Find the exact area of a circle with radius 3. **Answer:** 9π
Near the end of this topic, use A equals pi r squared, making sure r is the radius.

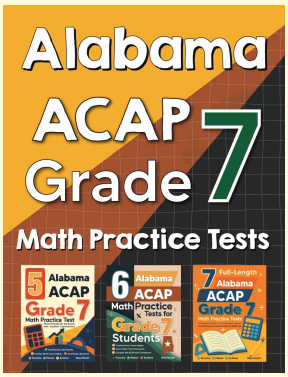
Word-problem notes:

16. Answer: A: $254.34\ m^2$; B: $452.16\ m^2$; difference: $197.82\ m^2$; A: $\approx 5.1\ hr$; B: $\approx 9.0\ hr$.
Find each pond area with $A = \pi r^2$. Pond A has area $\pi(9)^2 = 81\pi \approx 254.34\ m^2$, and Pond B has area $\pi(12)^2 = 144\pi \approx 452.16\ m^2$. Subtract to compare them: $452.16 - 254.34 = 197.82\ m^2$. To find the treatment time, divide each area by the crew's rate of $50\ m^2$ per hour. That gives about 5.1 hours for Pond A and 9.0 hours for Pond B.

17. Answer: Whole: $\pi(14)^2 \approx 615.44\ cm^2$; slice: $\approx 76.93\ cm^2$; volume: $\approx 384.6\ cm^3$.
Start by converting the diameter to radius: $28 \div 2 = 14\ cm$. The whole cake area is $\pi(14)^2 = 196\pi \approx 615.44\ cm^2$. Since the cake is cut into 8 equal slices, divide by 8 to get one slice area: about $76.93\ cm^2$. The slice volume is approximately area times height, so $76.93 \times 5 \approx 384.6\ cm^3$.

Want Even More Practice?

Check Out Our Other Alabama ACAP Test Books!



Alabama ACAP Grade 7 Math Preparation Bundle

18 full-length practice tests across three books (5 + 6 + 7)

No repeated questions—maximum practice value!

18 Tests!
3 Books
One Bundle

Important: All our test books contain **unique, completely different tests** from each other! Each book offers fresh practice questions—no repeats!

5 Practice Tests

- ✓ 5 complete practice tests with detailed explanations
- ✓ Perfect foundation for ACAP test preparation
- ✓ Builds confidence and test-taking skills
- ✓ High-quality questions aligned with state standards

Start your practice journey!

6 Practice Tests

- ✓ 6 complete practice tests with detailed explanations
- ✓ **Unique tests**—different from the 5 tests book
- ✓ Perfect for more practice after mastering 5 tests
- ✓ Builds even more confidence and test-taking skills
- ✓ Same high-quality questions aligned with standards

Take your practice to the next level!

7 Practice Tests

- ✓ 7 complete practice tests for maximum preparation
- ✓ **Unique tests**—different from 5 and 6 tests books
- ✓ The most comprehensive practice for Grade 7
- ✓ Ideal for students aiming for top scores
- ✓ Extensive practice builds mastery and confidence

Go all the way with comprehensive practice!